

Supplementary material

HEPTAGONAL QUASICRYSTALS: CONSTRUCTION OF 2D LATTICES AND DEMONSTRATIONS USING LASER POINTERS – CONCLUDING PART*

Vladimir M. Petruševski¹, Sašo M. Kalajdžievski²

¹ *Institute of Chemistry, Faculty of Natural Sciences and Mathematics,
Ss. Cyril & Methodius University in Skopje, Macedonia*

² *Department of Mathematics, University of Manitoba, Winnipeg, Canada*
vladop@pmf.ukim.mk, sasho.kalajdzievski@umanitoba.ca

The Mathematica program for generation the set of points

```
ListPlot[Union[
{{0, 0}},

(2/2) Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}],

(3/3) Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 1, 7}],

(4/4) Table[(1 + 2*Cos[4*Pi/14]) {Cos[n*al[7]], Sin[n*al[7]]}, {n,
1, 7}],

(5/5) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 1, 7}],

(6/6) Table[(1 + 2*Cos[4*Pi/14]) {Cos[n*al[7]], Sin[n*al[7]]}, {n,
1, 7}] + Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}],

(6/6) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
```

```

norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
    Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 1,
7}] + Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}],

(6/6) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 1,
7}] + Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}],

(7/7) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}],

(7/7) Table[(1 + 2*Cos[4*Pi/14]) {Cos[n*al[7]], Sin[n*al[7]]}, {n,
0, 6}] + Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}],

(7/7) Table[(1 + 2*Cos[4*Pi/14]) {Cos[n*al[7]], Sin[n*al[7]]}, {n,
0, 6}] + Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}],

(8/8) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}],

```

```
(8/8) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}],
```

```
(8/8)
Table[(1 + 2*Cos[4*Pi/14]) {Cos[n*al[7]], Sin[n*al[7]]}, {n, 0,
6}] + Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}],
```

```
(9/9) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}],
```

```
(9/9) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}],
```

(9/9)

```
Table[(1 + 2*Cos[4*Pi/14]) {Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] + Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}],
```

(10/10) Table[(2*Cos[3*Pi/7] +

```
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}], {n, 0,
6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}],
```

(10/10) Table[(2*Cos[3*Pi/7] +

```
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}],
```

(11/11) Table[(2*Cos[3*Pi/7] +

```
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
```

```
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}],
```

(12/12)

```
Table[(1 + 2*Cos[4*Pi/14]) {Cos[n*al[7]], Sin[n*al[7]]}, {n, 0,
6}] + Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}],
```

(12/12)

```
Table[(1 + 2*Cos[4*Pi/14]) {Cos[n*al[7]], Sin[n*al[7]]}, {n, 0,
6}] + Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}],
```

(13/13) Table[(2*Cos[3*Pi/7] +

```
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}],
```

(13/13) Table[(2*Cos[3*Pi/7] +

```
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}],
```

```

Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}],

```

```

(14/14) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}}], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}],

```

```

(14/14) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}}], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}],

```

```

(14/14) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]})/

```

```

norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
    Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
    Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
    Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}],

```

(15/15)

```

Table[(1 + 2*Cos[4*Pi/14]) {Cos[n*al[7]], Sin[n*al[7]]}, {n, 0,
6}] + Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}],

```

(16/16) Table[(2*Cos[3*Pi/7] +

```

2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
    Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
    Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
    Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
    Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}],

```

(16/16) Table[(2*Cos[3*Pi/7] +

```

2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
    Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
    Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}),

```

```

Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{{Cos[n*al[7]], Sin[n*al[7]]}}, {n, 2, 8}] +
Table[{{Cos[n*al[7]], Sin[n*al[7]]}}, {n, 1, 7}],

(16/16) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0,
6}] + Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{{Cos[n*al[7]], Sin[n*al[7]]}}, {n, 2, 8}] +
Table[{{Cos[n*al[7]], Sin[n*al[7]]}}, {n, 6, 12}] +
Table[{{Cos[n*al[7]], Sin[n*al[7]]}}, {n, 1, 7}],

(16/16) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0,
6}] + Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{{Cos[n*al[7]], Sin[n*al[7]]}}, {n, 2, 8}] +
Table[{{Cos[n*al[7]], Sin[n*al[7]]}}, {n, 6, 12}]

```

```

Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}],

(17/17) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}],

(17/17) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}],

(17/17)
Table[(1 + 2*Cos[4*Pi/14]) {Cos[n*al[7]], Sin[n*al[7]]}, {n, 0,
6}] + Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}]

```

```

Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}],

(18/18) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}],

(18/18) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}],

(18/18) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}], {n, 0,
6}]

```

```

6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}],

(19/19) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}],

(19/19) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +

```

```
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}],
```

(19/19)

```
Table[(1 + 2*Cos[4*Pi/14]) {Cos[n*al[7]], Sin[n*al[7]]}, {n, 0,
6}] + Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}],
```

(19/19)

```
Table[(1 + 2*Cos[4*Pi/14]) {Cos[n*al[7]], Sin[n*al[7]]}, {n, 0,
6}] + Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}],
```

(20/20) Table[(2*Cos[3*Pi/7] +

```
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
```

```

Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}],

(20/20) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}],

(20/20)
Table[(1 + 2*Cos[4*Pi/14]) {Cos[n*al[7]], Sin[n*al[7]]}, {n, 0,
6}] + Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}],

(21/21) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}]

```

```

Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}],

(21/21) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}],

(21/21) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}].{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +

```

```

Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}],

(21/21) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}],

```

```

(22/22) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[{{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +

```

```

Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}],

(22/22) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}],

(21/21) Table[(2*Cos[3*Pi/7] +
2 Cos[Pi/
7])*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})/
norm[({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]})], {n, 0,
6}] + Table[
2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[2 Cos[al[7]/
2]*({{Cos[al[7]/2], -Sin[al[7]/2]}, {Sin[al[7]/2],
Cos[al[7]/2]}}.{Cos[n*al[7]], Sin[n*al[7]]}), {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 2, 8}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 1, 7}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 0, 6}] +
Table[{Cos[n*al[7]], Sin[n*al[7]]}, {n, 6, 12}]

```

],

AspectRatio -> True, Axes -> False,
PlotStyle -> {PointSize[0.02], Black}]