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Original scientific paper

SUPPLEMENTARY MATERIAL

DECODING THE FEATURES OF BIOCHEMICAL MULTISTEP ELECTRON-TRANSFER PATHWAYS WITH THE TWO-STEP DOUBLE- REGENERATIVE ELECTROCHEMICAL MECHANISM IN SQUARE-WAVE VOLTAMMETRY

Rubin Gulaboski

Faculty of Medical Sciences, Goce Delčev University, Štip, North Macedonia

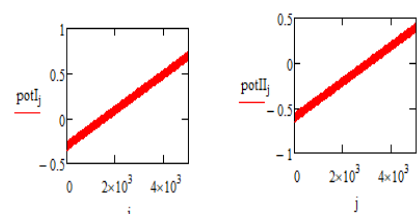
rubin.gulaboski@ugd.edu.mk

Two-step Double-regenerative EC'EC'' Mechanism in SWV

$E_{sI} := -0.4$ $\Delta E := 1$ $dE := 0.01$ $E_{sw} := 0.05$ $f := 10$ $E_{sII} := -0.7$ $r := 1..1$
 $n := 1$ $F := 96500$ $R := 8.314$ $T := 298.15$ $\alpha_1 := 0.5$
 $j := 1.. \frac{\Delta E}{dE} \cdot 50$ $ks1 := 0.1$ $\alpha_2 := 0.5$
 $ks2 := 0.1$
 $D := 0.000005$

$$potI_j := (E_{sI} + E_{sw}) + \left[\left[\text{ceil} \left(\frac{j-1}{25} \right) \cdot dE + \text{if} \left(\frac{\text{ceil} \left(\frac{j}{25} \right) = \text{ceil} \left(\frac{j-1}{25} \right), 1, -1 \right) \cdot E_{sw} + E_{sw} \right] - dE \right]$$

$$potII_j := (E_{sII} + E_{sw}) + \left[\left[\text{ceil} \left(\frac{j-1}{25} \right) \cdot dE + \text{if} \left(\frac{\text{ceil} \left(\frac{j}{25} \right) = \text{ceil} \left(\frac{j-1}{25} \right), 1, -1 \right) \cdot E_{sw} + E_{sw} \right] - dE \right]$$



$$\Phi_{I_j} := n \cdot \frac{F}{R \cdot T} \cdot potI_j \quad \Phi_{II_j} := n \cdot \frac{F}{R \cdot T} \cdot potII_j$$

$$\Psi_{I_1} := \frac{K1 \cdot e^{\alpha_1 \cdot \Phi_{I_1}}}{1 + K1 \cdot Kchem1 \cdot e^{-\frac{5}{2} \cdot \alpha_1 \cdot \Phi_{I_1}} \cdot \left(1 + e^{-\Phi_{I_1}} \right)}$$

$$\Psi_{II_1} := \frac{Kchem1 \cdot e^{-\frac{5}{2} \cdot \alpha_2 \cdot \Phi_{II_1}} \cdot \Psi_{I_1} \cdot A_1}{1 + K2 \cdot A_1 \cdot e^{\alpha_2 \cdot \Phi_{II_1}} \cdot \left(1 + e^{-\Phi_{II_1}} \right)}$$

$$\Psi_{I_1} = 8.082 \times 10^{-6}$$

$$\Psi_{II_1} = 0$$

$$\frac{f}{\omega} := 10$$

$$kc1 := 100$$

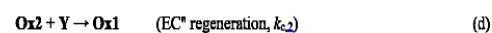
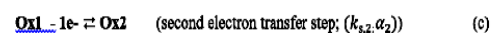
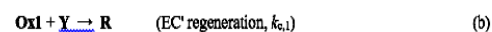
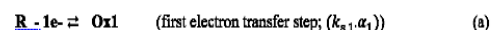
$$kc2 := 200$$

$$K1 = \frac{ks1}{(D \cdot f)^{0.5}}$$

$$K2 = \frac{ks2}{(D \cdot f)^{0.5}}$$

$$Kchem1 = \frac{kc1}{f}$$

$$Kchem2 = \frac{kc2}{f}$$



Meaning of the symbols of defined parameters:

- kc_1 and kc_2 are the rate constants of first and second regenerative step, respectively

- $Kchem1$ and $Kchem2$ are dimensionless chemical (regenerative) parameters related to the first and second regenerative step, respectively

- $K1$ and $K2$ are dimensionless rate parameters related to the first and second electron transfer step, respectively

- $ks1$ and $ks2$ are standard rate constants of first and second electron transfer steps, respectively

- Φ_I and Φ_{II} are dimensionless potentials

- D is symbol for the diffusion coefficient (assumed to be identical for all redox active species involved in the mechanism)

- j is serial number of time increments

A_j B_j are numerical integration parameters

- n is number of electrons exchanged

- dE is potential step

- E_{sw} is square-wave amplitude

- f is SW frequency

- E_{sI} and E_{sII} are standard potential of first and second electron transfer step, respectively

- α_1 and α_2 are electron transfer coefficients related to the first and second electron transfer step, respectively

- F , R and T are Faraday constant, Gas constant and temperature, respectively

- $potI$ and $potII$ are potential modulations related to the first and second electron transfer step, respectively

- Ψ is symbol for the dimensionless current

Entire simulation protocol for calculating square-wave voltammograms in Mathcad is available for free in:

Gulaboski, R.; Mirceski, V. J. Solid State Electrochem. Square-Wave Voltammetry of Two-Step Diffusional Electrode Mechanism Coupled with a Reversible Follow-Up Chemical Reaction. *J. Solid State Electrochem.* **2021**, *25*, 2893-2901. <https://doi.org/10.1007/s10008-021-05027-4>

30 days free trial version of Mathcad available at:

<https://support.ptc.com/products/mathcad/mathcad-15-0/free-trial?refid=cadventure>

$$\Psi I_j = \frac{K1 \cdot e^{\alpha1 \cdot \Phi I_j} \left[1 - \frac{1 + e^{-\Phi I_j}}{\sqrt{Kchem1}} \sum_{i=1}^{j-1} (\Psi I_i \cdot A_{j-i+1}) \right]}{1 + K1 \cdot \frac{1}{\sqrt{Kchem1}} \cdot A_1 \cdot e^{\alpha1 \cdot \Phi I_j} \cdot (1 + e^{-\Phi I_j})}$$

$$\Psi II_j = \frac{K2 \cdot \frac{1}{\sqrt{Kchem1}} \cdot e^{\alpha2 \cdot \Phi II_j} \sum_{i=1}^j (\Psi I_i \cdot A_{j-i+1}) - \frac{1}{\sqrt{Kchem2}} \cdot K2 \cdot e^{\Phi II_j \cdot \alpha2} \sum_{i=1}^{j-1} (\Psi II_i \cdot B_{j-i+1}) - \frac{1}{\sqrt{Kchem2}} \cdot K2 \cdot e^{-\Phi II_j \cdot (1-\alpha2)} \sum_{i=1}^{j-1} (\Psi II_i \cdot B_{j-i+1})}{1 + \frac{1 \cdot B_1}{\sqrt{Kchem2}} \cdot K2 \cdot e^{\Phi II_j \cdot \alpha2} + \frac{1 \cdot B_1}{\sqrt{Kchem2}} \cdot K2 \cdot e^{-\Phi II_j \cdot (1-\alpha2)}}$$

$$\Psi_j = \Psi I_j + \Psi II_j$$

$$p = 1 - \left(\frac{\Delta E}{dE} \right) - 1$$

$$\Psi If_p = \Psi I_{(p+1) \cdot 50} \quad \Psi Ib_p = \Psi I_{50 \cdot p + 25} \quad \Psi Inet_p = \Psi If_p - \Psi Ib_p$$

$$\Psi IIb_p = \Psi II_{50 \cdot p + 25} \quad \Psi II f_p = \Psi II_{(p+1) \cdot 50} \quad \Psi II net_p = \Psi II f_p - \Psi II b_p$$

$$E_p = Esl + p \cdot dE$$

$$\Psi b_p = \Psi_{50 \cdot p + 25} \quad \Psi f_p = \Psi_{(p+1) \cdot 50} \quad \Psi net_p = \Psi f_p - \Psi b_p$$

